Quadric Surface: The graph of the equation

$$
A x^{2}+B y^{2}+C z^{2}+D x y+E y z+F x z+a x+b y+c z+d=0
$$

in $\mathbb{R}^{3}$ (three-dimensional space), where $A, B, C, D, E, F, a, b, c, d$ are constants and at least one of $A, B, C, D, E, F$ is not zero, is called a quadric surface.

1. Traces (Cross-Sections): Traces are curves of intersection of the surface with planes parallel to the coordinate planes.
2. Cylindrical Surface: Cylinders are surfaces whose traces in every plane parallel to a given plane are the same.
3. Sketch the surface $x^{2}+\frac{y^{2}}{4}+\frac{z^{2}}{9}=1$.
4. Sketch the surface $x^{2}+y^{2}=z$.
5. Sketch the surface $x^{2}+\frac{y^{2}}{4}=z^{2}$.
6. Sketch the surface $\frac{x^{2}}{4}+y^{2}-\frac{z^{2}}{2}=1$.
7. Sketch the surface $\frac{x^{2}}{4}-y^{2}-\frac{z^{2}}{2}=1$.
8. Sketch the surface $z=2 y^{2}-x^{2}$.
9. Describe the surface $4 x^{2}+4 y^{2}+z^{2}+8 y-4 z+4=0$.
10. Identify the surfaces (a) $3 x^{2}-4 y^{2}+12 z^{2}+12=0$ and (b) $4 x^{2}-4 y+z^{2}=0$.
11. (833) \#41. Sketch the region bounded by the surfaces $z=\sqrt{x^{2}+y^{2}}$ and $x^{2}+y^{2}=1$ for $1 \leq z \leq 2$.
12. Match the graph with the appropriate equation below:

(a) $x^{2}+4 y^{2}+9 z^{2}=1$
(b) $9 x^{2}+4 y^{2}+z^{2}=1$
(c) $3 x^{2}+3 y^{2}+3 z^{2}=1$
(d) $x^{2}-y^{2}+z^{2}=1$
(e) $-x^{2}+y^{2}-z^{2}=1$
(f) $y=2 x^{2}+z^{2}$
(g) $y^{2}=2 x^{2}+z^{2}$
(h) $x^{2}+2 z^{2}=1$
(i) $y=x^{2}-z^{2}$
13. A cooling tower for a nuclear reactor is to be constructed in the shape of a hyperboloid of one sheet. The diameter at the base is 280 meters and the minimum diameter, 500 meters above the base, is 200 meters. Find an equation for the tower.


| Ellipsoid $\left(\frac{x}{a}\right)^{2}+\left(\frac{y}{b}\right)^{2}+\left(\frac{z}{c}\right)^{2}=1$ | Hyperboloid (one sheet) $\left(\frac{x}{a}\right)^{2}+\left(\frac{y}{b}\right)^{2}=\left(\frac{z}{c}\right)^{2}+1$ | Hyperboloid (two sheets) |
| :---: | :---: | :---: |
| Elliptic Paraboloid | Hyperbolic Paraboloid | Cone |
| Elliptic Cylinder | Hyperbolic Cylinder | Parabolic Cylinder |

